MODELING AND FE ANALYSIS OF FUNCTIONALLY GRADED (FG) COMPOSITE SHELL STRUCTURES

Rajat Yadav¹, Anas Islam¹, Kamal Sharma¹

¹IET Department of Mechanical Engineering GLA University Mathura – 281406
Corresponding Author- rajat.yadav@glu.ac.in

Abstract
This manuscript comprises with FG (functionally graded) analysis and finite modeling element shell frameworks under divergent loading like mechanical & thermal. The analysis of free vibration of FG spherical shell framework has also been depicted. In respect to research the impact of significant aspects on FG shell frameworks responses, divergent kinds of shells were deliberated. Here, responses were attained for FG shells were compared to pure ceramic homogeneous shells (Al2O3) and EN 31 Steel (pure metal) and it is perceived that FGM Shells responses were in between homogenous shells responses. Furthermore, static analysis done on FG shell structure is to determine the circumferential and longitudinal stress, strain and deformation. Furthermore, modal analysis is to be determining the natural frequencies.

Keywords: EN 31 steel alloys, Al2O3, FG, ceramic, CATIA and ANSYS

1. Introduction
Different domains of engineering, for example, aerospace, mechanical, civil and atomic designing fields the meager walled tube-shaped shells find more extensive applications as essential structural individuals [1-4]. The solidified and un hardened shells comprised of metallic and covered composite materials (enormous breadth to thickness proportion) are broadly utilized in space vehicles, submerged, air, surface, and just as in development of weight vessels, stockpiling vessels, stockpiling containers and fluid stockpiling tanks [5-7]. The mathematical flaws because of assembling measures takes predominant job in diminishing the clasping heap of barrel shaped shells. Buckling is frequently seen as the controlling disappointment method of these structures because of its generally little thickness of these basic members. It is hence fundamental that the clasping quality of the slight shells alongside information on its buckling has been the subject of numerous scientists in both expository and experimental investigations [8-12].

Structures of Composite are significant in various territories of industry, for example, marine ships, airplanes, car [13-15]. Most of the frameworks understand the blast stacking during war or psychological oppressor assault or coincidental blasts [16]. Reaction of composite structures exposed to blast has been a field of extraordinary action of scientists in ongoing decades [17]. Therefore, the structures of shells and composite plates are one of the essential components of the structures, consequently, examining the shoot reaction of such structures assists in understanding and enhancing their blast resistance.

Functionally Graded Materials (FGM)
FGMs are a gathering of inhomogeneous materials made out of at least two materials designed to have
Persistently changing material properties along favored headings. The FG materials are infinitesimally heterogeneous and are produced using blend of at least two materials that are fitting to accomplish the ideal targets. The general material properties of the FGMs are extraordinary and not the same as the individual material that structures. The mechanical properties, which shift consistently in the favored ways, are Shear Modulus Young's modulus, Shear Modulus and thickness, Poisson's proportion, and so forth. Figure 1 exhibits a bar made of such FG material made out of two materials, earthenware and metal. The top and base surfaces of this FG shaft are viewed as clay and metal rich, separately, and the material properties differ over its thickness in a smooth and ceaseless way. Such a bar can withstand high temperature slope over its thickness while keeping up the fracture toughness.

The clay rich surface presented to maximum temperature gives warm opposition because of its low warm conductivity while the metallic constituent gives sturdiness of the plate.

![Fig 1. Schematic representation of FG beam](image)

2. LITERATUREREVIEW

**Reza Haghi** [1] In this manuscript, the conduct of composite structures against the dangerous marvel has been examined utilizing limited component technique. Some composite shells, for example, composite plates and sides of the equator with various layer-increasing have been explored utilizing LS-DYNA programming. The impact stacking is recreated by blast's weight versus time bends and is straightforwardly characterized in LS-DYNA programming. The Tsai-Wu disappointment model is utilized to anticipate the conduct of the composite structure. In this paper, the impact of layer-increasing on the shoot obstruction of the structure is examined. The outcomes show that, side of the equator composite has better execution against the shoot stacking than plate and disappointment happen under more noteworthy burden. Additionally, it is demonstrated that point handle composite structures have great obstruction in examination with cross pliesone.

**Mahmoud Shariati** [2] In this article, the impacts of the length, division edge and diverse limit conditions on the clasping burden and post clasping conduct of CK20 round and hollow boards have been investigated. The mathematical outcomes are in acceptable concurrence with the simulation tests.

**M. Shariati** [3] The impacts of diverse limit, length and division edge conditions on the post buckling conduct and burden of barrel shaped boards have been researched utilizing exploratory and mathematical strategies. The trial tests have been performed utilizing a servo water driven machine & for mathematical investigation, Abaqus limited component bundle has been utilized. The mathematical outcomes are in acceptable concurrence with the simulation tests.

**Y. VenkataNarayana** [4] Dainty round and hollow shells and boards are more inclined to bomb in clasping instead of material disappointment. In this current investigation direct and non-straight clasping
examination of GFRP barrel shaped shells under pivotal pressure is done utilizing broadly useful limited component program (ANSYS). Cutoff point loads assessed for mathematical defect extents shows a great concurrence with trial results [25]. The impact of composite tube-shaped shell thickness, radius variation on clamping load and clamping mode has additionally researched. Present examination finds direct application to explore the impact of mathematical defects on other progressed matrix stiffened structures.

3. REVIEW OF SHELL THEORIES

All in all, shell structures are portrayed as the three-dimensional bodies limited by two, generally close, bended surfaces. The greater part of the shell speculations (slender and thick, profound and shallow) decreases the three-dimensional flexibility conditions to the two-dimensional portrayal. This is commonly done by disposing of the organize typical to the shell surface in the advancement of the shell conditions. The exactness of slender and thick shell speculations can be set up if these hypotheses are contrasted with the three-dimensional hypothesis of elasticity.

In this area the continuous course of shell research is introduced. For clear understanding of the orderly and sequential improvement of the various parts of shell research, this segment is additionally isolated into particular parts referenced beneath.

Objective

The pressure appropriation of FGM made barrel shaped shell for given burden conditions must be broke down. Thus, in this work, displaying and basic investigation have been done on an evaluated tube shaped shell with changing natural arrangement from internal surface to the external surface. Conveyance of volume portion of the components is determined utilizing power law for tube shaped shell demonstrating. Static basic examination of round and hollow shell which is presented to inward weight performed and results are checked with diagnostic arrangements.

4. METHODOLOGY

![Fig 2. Schematic diagram of cylindrical shell.](image-url)
MODELING AND ANALYSIS

CATIA is an abbreviation for Computer Aided Three-dimensional Interactive Application. It is one of the main 3D programming utilized by associations in various enterprises going from aviation, car to buyer items. CATIA is a multi-stage 3D programming suite created by Dassault Systems, including CAD, CAM just as CAE. Dassault is a French building monster dynamic in the field of flight, 3D plan, 3D computerized models, and item lifecycle the executives (PLM) software.

Round and hollow shell hypothetical detailing

Beneath Fig. Shows the schematic graph of round and hollow shell organizes with heading of x, θ, & z for pivotal, radial and circumferential bearings individually. The calculation of shell is 1500 mm length, 1500 mm inside span, and 15 mm thickness.

Material Properties Calculations For FGM

**Nomenclature**

\[ E_t = \text{Top material young’s modulus (N/mm}^2) \]

\[ E_b = \text{bottom material young’s modulus (N/mm}^2) \]

\[ \rho_t = \text{Top material density (Kg/mm}^3) \]
$\rho_b =$ bottom material density (Kg/mm$^3$) $k =$ coefficient factor

$Z =$ Layer stacking number \textbf{For Young's Modulus} $E(Z) = (E_t - E_b) (z/h + 1/2)^k + E_b$ \textbf{For}

\textbf{Densities}

$\rho (Z) = (\rho_t - \rho_b) (z/h + 1/2)^k + \rho_b$

\textbf{Table.} Functionally graded material properties (aluminum alloy and ceramic) for $k=2$

<table>
<thead>
<tr>
<th>Layer number($z$)</th>
<th>Young's modulus $E$ (MPa)</th>
<th>Density $\rho$ (Kg/m$^3$)</th>
<th>Poisson ratio $\nu$</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>220880</td>
<td>5536</td>
<td>0.31</td>
</tr>
<tr>
<td>4</td>
<td>320720</td>
<td>4830</td>
<td>0.309</td>
</tr>
<tr>
<td>3</td>
<td>445520</td>
<td>4164</td>
<td>0.308</td>
</tr>
<tr>
<td>2</td>
<td>595280</td>
<td>3702</td>
<td>0.307</td>
</tr>
<tr>
<td>1</td>
<td>770000</td>
<td>3307</td>
<td>0.306</td>
</tr>
<tr>
<td>-1</td>
<td>96080</td>
<td>2812</td>
<td>0.304</td>
</tr>
<tr>
<td>-2</td>
<td>71120</td>
<td>2711</td>
<td>0.303</td>
</tr>
<tr>
<td>-3</td>
<td>71120</td>
<td>2711</td>
<td>0.302</td>
</tr>
<tr>
<td>-4</td>
<td>96080</td>
<td>2812</td>
<td>0.301</td>
</tr>
<tr>
<td>-5</td>
<td>146000</td>
<td>2383</td>
<td>0.3</td>
</tr>
</tbody>
</table>

Table: material properties of EN 31 steel
Case: 1 cylindrical shell LAYERS

<table>
<thead>
<tr>
<th>Layer</th>
<th>Material</th>
<th>Thickness (mm)</th>
<th>Angle (°)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>EN3</td>
<td>206000</td>
<td>430</td>
</tr>
<tr>
<td>1</td>
<td>Steel</td>
<td>0.29</td>
<td>0.000000</td>
</tr>
<tr>
<td>1</td>
<td>430</td>
<td>70</td>
<td>70</td>
</tr>
</tbody>
</table>

Directional deformation

Circumferential Stress

Longitudinal stress

<table>
<thead>
<tr>
<th>Material</th>
<th>Young’s modulus (MPa)</th>
<th>Tensile strength (MPa)</th>
<th>Poisson’s ratio</th>
<th>Density (kg/mm³)</th>
<th>Strain</th>
</tr>
</thead>
</table>
Case: 2 Cone Shell Directional deformation

Circumferential Stress

Longitudinal stress

Strain

Table: FG material results of cylindrical and cone shell structures
### MODAL ANALYSIS OF SHELL

**5. STRUCTURES**

**CASE: 1 CYLINDRICAL SHELL**

Total deformation 1

<table>
<thead>
<tr>
<th>Shell</th>
<th>Direct deformation (mm)</th>
<th>Circumferential stress (N/mm²)</th>
<th>Longitudinal stress (N/mm²)</th>
<th>Strain (N/mm²)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cyindrical</td>
<td>3</td>
<td>52.83</td>
<td>53.28</td>
<td>0.000</td>
</tr>
<tr>
<td>Cone</td>
<td>2.2004</td>
<td>34.35</td>
<td>32.621</td>
<td>0.001</td>
</tr>
</tbody>
</table>

Total deformation 2

Total deformation 3
CASE: 2 CONE SHELL

Total deformation 1

Total deformation 2

Total deformation 3

Table: modal analysis results of shell structures

<table>
<thead>
<tr>
<th>shell struct</th>
<th>Defo</th>
<th>Fre</th>
<th>Defo</th>
<th>Fre</th>
<th>Defo</th>
<th>Fre</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cyl</td>
<td>0.98</td>
<td>56</td>
<td>0.98</td>
<td>56</td>
<td>1.03</td>
<td>66</td>
</tr>
</tbody>
</table>
Graph: frequency values of cylindrical and cone shell structures.

Graph: circumferential stress values of cylindrical and cone shell structures with EN 31 and FGM materials

Graph: longitudinal stress values of cylindrical and cone shell structures with EN 31 and FGM materials

6. CONCLUSION

Static auxiliary investigation for a tube shaped and cone shell was done for single material structure and FGM made structure. The reviewed structure material properties and volume divisions are determined by utilizing power law. For each layer, volume portion material properties are given to reproduction model.
Static auxiliary investigation of tube shaped and cone shell with inward weight load was performed for both single material and reviewed material structure. Reproduction aftereffects of single material are checked with the investigative arrangement and found that rate mistake is less. Henceforth a similar cycle embraced for FGM made tube shaped and cone shell. Reenactments performed to assess circumferential and longitudinal pressure dispersions in FGM made shell. It was seen that the evaluated structure shows preferred execution over the single material framework at shell structure of cone.

REFERENCES

3. B. Prabu, N. Rathinam, R. Srinivasan,