

DTW SIMILARITY MEASURE BASED U-SHAPELETS CLUSTERING ALGORITHM FOR TIME-SERIES DATA

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Abstract

Time-Series Analysis exhibited efficient results in delivering significant knowledge in numerous domains. Most of the investigation on Time-Series Analysis is restricted with the requirement of expensive categorized information. This led to the growth of curiosity in grouping the time-series information that does not need any access to categorized information. The clustering time-series information carries out issues that do not prevail in conventional clustering methodologies, in the Euclidean space amongst the objects. Therefore, the authors suggested an innovative clustering technique, for Time-Series employing of DTW similarity measure by extracting unsupervised shapelets. And these extracted u-shapelets are clustered employing iterative k-means algorithm. The DTW similarity measure provides better accuracy in formed clusters of proposed methodology compared to the Metric Euclidean Distance Measure. The performance of the suggested approach is evaluated employing the Rand Index (RI) Measure. The experimental for this approach was performed on four different Time-Series data samples and the outcomes showed that the RI measure for the DTW based Time-Series Clustering Algorithm is more when compared to the Existing ED-based Time-Series Clustering Algorithm.

Keywords: Time-Series Analysis, Clustering, Unsupervised Shapelets, K-means, Dynamic Time Warping

1. Introduction

A Time-Series is a gathering of interpretations relating to the sequential arrangement. The environment of time-series information could be categorized through features such as huge data magnitude, high magnitude, and the necessity for constant updating. The aim of Time-Series analysis is normally divided into folds: to know or produce the stochastic technique that bounces to a perceived sequence and to forecast the upcoming values of sequence aided past sequence and conceivably other associated series of aspects. The previous decade has perceived emerging importance in grouping approaches for time series data to enable innovative appliances in numerous domains like bioinformatics ^[1,2,3], ecological monitoring ^[4], financial applications ^[5], etc.

Clustering Time-Series and other series of information have been a significant domain inspired through numerous studies comprising identical exploration in addition to challenges of producing approaches to distinguish dynamic changes in Time-Series. Time series clustering targets detecting configuration in an un-categorized Time-Series data sample through empirically establishing information into homogeneous clusters where the resemblances among objects in a similar group are increased and the resemblances among identities across clusters are decreased^[6]. The fascinating shapes concealed in a Time-Series sample could be known through reviewing the clusters exposed using the clustering techniques. Most of the Time-Series clustering approaches disapprovingly hinge on the selection of a similarity distance measure, and these procedures habitually estimate likenesses among Time-Series entities relating to complete series. Nevertheless, it is further rationale to assess the resemblance among two Time-Series elements pertaining to a fragment of a time intermission alternative to complete series for higher-dimensional Time-Series clustering in numerous appliances.

Time-Series analysis is a vital domain inside numerous areas of study comprising aerospace, economics, commerce, weathercasting, medical science, motion capture, etc.^[7]. Information attained through observations gathered serially over the period is widely common^[8]. Incorporate, weekly interest rates, everyday concluding stock charges, periodic price catalogs, an annual sales figure, and further are observed. In weathercasting, everyday higher and lower costs, annual rainfall and famine catalogs, and hourly wind power are observed. In agriculture, yearly statistics for harvest and live stocks generation, soil erosion, and export trades are recorded. Inorganic science, the electrical activities at millisecond intermissions are recorded. In an ecosystem, plenty of animal types are recorded. The list of the domain where Time-Series are studied is infinite.

Numerous clustering algorithms are introduced in the earlier few years specifically for Time-Series datasets where the maximum of the clustering techniques employ the linear method for similarity checks such as metric Euclidean Distance, City Block Distance, Manhattan Distance, etc. The approaches give good results for the traditional databases whereas produces very poor results for the Time-Series data samples where the class labels are not known. The linear similarity measures perform better results when the span of different time objects is equal and have no misrepresentation in the time axis. Due to this, the Time-Series data are pruned to obtain equal length for clustering, and the maximum of the evidence is lost.

Therefore, so as to overcome the above-mentioned issue, an innovative cluster technique is introduced by initially extracting the unsupervised shapelets from the unequal Time-Series dataset and employing these u-shapelets for the cluster the Time-Series data. Different from the existing clustering algorithm where linear similarity distances are employed, in this investigation, a non-linear similarity measure is known as Dynamic Time Warping (DTW) is employed to estimate the distance amongst different Time-Series objects. DTW addressed the issue of distortion in the time-axis. DTW techniques evaluate the distance of two uneven sized Time-Series fragments through arranging the signals employing energetic program design depending on constrictions to accommodate those that are identical, however locally out of phase, as shown in Figure 1.

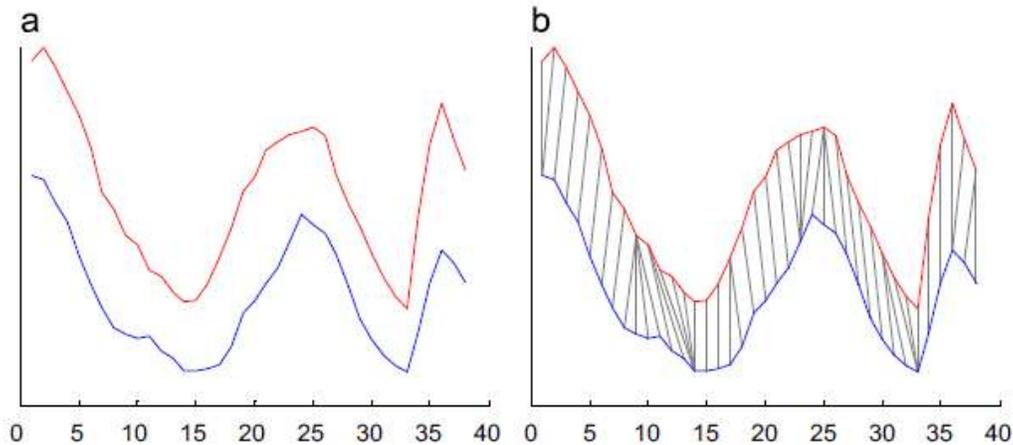


Figure 1: Arrangement of Series using DTW (a) two comparable Sequences out of phase (b) arrangement using DTW

1.1 Organization of the paper

A brief discussion on the introduction of the Time-Series analysis and motivation for the proposed approach is given in this section. Section 2 gives briefly explains the existing approaches in the Time-Series analysis for clustering using different techniques. The unsupervised shapelets for the cluster of the Time-Series data are briefly explained in section 3. The suggested DTW based U-Shapelets Clustering Algorithm is briefly given in section 4.

2. Literature Survey

Contemporary approaches detect shapelets by demanding a pond of applicant sub-series from entire probable sequential fragments^[9, 10] and formerly arranging the topmost executing fragments pertaining to its destination forecasting abilities. Distances amongst sequence and shapelets exhibit shapelet-transmuted^[10] categorization features for a serial fragmentation metrics like information gain^[9, 11], FStat^[12] or Kruskal-Wallis^[13]. The brute-force applicant explore methodologies depending on an extensive examination of applicants, suffers from a higher execution time complexity, hence numerous rapidly employed approaches are intended at minimizing the detection period of Shapelets^[11, 14, 15]. Identical to stable data clustering, Time-Series needs a clustering procedure to generate groups for the specified group of un-categorized data elements and the selection of clustering approaches hinges on the kind of information accessible and on the specific function and application.

For clustering multimedia Time-Series,^[16] accomplished K-means and K-medoid techniques having DTW and showed that K-means is a standard clustering approach whenever Euclidean distance is employed, however, it becomes an unsuccessful attempt to attain accurate outcomes while DTW is employed as a distance measure in summarizing the structure of the Time-Series. As an outcome of the experimentations, this guaranteed that DTW

must not be employed like a subroutine using the K-means approach and K-medoids using DTW obtaining adequate outcomes.

A new technique is defined in ^[17] for Time-Series clustering where DFT is employed to transfer time-series information from time to frequency channel. Considering, the transmuted amplitude of power band as the characteristics instance of the Time-Series information, it could be plotted to a frequency region. OPTICS (Ordering Points to Identify the Cluster Structure) approach is employed to identify groups in this information. Numerous replications are specified depending on the past California power marketplace.

In ^[18], k-Shape, an approach for time-series grouping is suggested. K-Shape hinges on an ascendant repetitive modified technique that produced standardized and well-segregated clusters. Considering the distance measure, k-Shape employed a standardized form of the cross-association so as to attain the structure of Time-Series when matching them. Depending on features of the distance measure, the methodology to estimate cluster centroids are presented that are employed in each generation to upgrade the Time-Series tasks to groups. Generally, k-Shape is an area autonomous, precise, and accessible methodology.

In ^[19], a novel variant of DTW distance measure for Time-Series structure summarizing categorization is suggested. Pertaining to this, resampled DTW and Hybrid DTW provide improved accurateness and high efficiency when compared to native DTW however to enhance the exactness additional, they suggested Contrast-Enhanced DTW (CEDTW) that minimized the influence of data points having non-trivial support to the distance and augmented the efficiency of the similarity measure.

In ^[20], a novel procedure for structure-aided Time-Series clustering is presented. It minimized the dimension of data, enhanced the effectiveness, and does not diminish the effect through employing the standard of the multifaceted network. Initially, the one-nearest neighbor network is constructed depending on the likeness amongst Time-Series entities. From the adjacent network, every node signifies a single Time-Series entity and every association refers to adjoin connection amongst nodes. Subsequently, the nodes having higher degrees are preferred and employed to the group. In the clustering technique, the DTW distance function and hierarchical grouping approach have functioned. Then, certain trails are implemented on artificial and real-world samples. The outcomes exhibited that the suggested technique has worthy performance on competence and efficiency.

A parsimonious prototype aided standard for grouping time sequence information is given in ^[28]. In this technique, the evaluation burden attains frequently a problem pertaining to huge accessible interpretations. The estimated Time-Series could likewise be low and scarce and a suitable prototype explaining them could become complex to determine. The technique is suggested to generate the viewed measurements through P-splines smoothers and formerly to collect these useful entities precisely using optimum spline coefficients. Giving the features of witnessed dimensions, the approach is merged with the appropriate grouping technique. The applications are offered depending on non-hierarchical grouping approaches. The accurateness and effectiveness of the suggested are estimated through simulations and through studying two real-world data instances.

A novel k -means a form of smooth subspace clustering technique known as Time-Series k -means for clustering is presented in ^[21]. This algorithm efficiently exploited intrinsic space data of a Time-Series to improve clustering efficiency. Further precisely, the horizontal subspaces are signified with weighted time stamps that specified a comparative discriminative signal of the timestamps for grouping entities. The foremost assistances of this study comprise the approach of the novel fitness function to assist the grouping of time-series information and expansion of new apprising guidelines to generate group exploration pertaining to even subspaces. Depending on the artificial samples and five practical samples, the experimental outcomes ratify that the suggested procedure outstrips other advanced Time-Series clustering approaches with the mutual performance metrics like Accuracy, Fscore, RandIndex, and Usual Mutual Information.

3. Time-Series Unsupervised Shapelets (U-Shapelets)

Time-Series Shapelets, a data mining primitive are Time-Series sub-sequences which in a certain manner excellently characteristic of a label^[9] and discriminative subsequences of Time-Series that finely forecast the destination value. Shapelets could offer interpretable outcomes that might assist the region expert's better knowledge of its information. It could be considerably further accurate and strong on certain data samples. This is since they are local characteristics, while maximum state-of-art Time-Series or shape classifiers/clustering functions on universal characteristics that could be delicate to even lower levels of noise and misrepresentations^[22]. Furthermore, detecting shapelets is a burning area in the time-series domain for the period of the previous five years ^[10, 11, 14].

The shapelets could likewise be extremely economical in clustering the time-series information. Since classes of Time-Series for clustering samples are not known, this leads to the issue of how the shapelets that can be discovered from data samples deprived of having information on the class labels. This issue proposed a novel kind of shapelet known as unsupervised-shapelet (or u-shapelet) and demonstrated the effectiveness of grouping time-series information^[23]. Since labels of Time-Series cannot be used to identify the shapelets, a description of informative subsequences is known as unsupervised-shapelets to distinguish them from the traditional shapelets that presume admittance to class names. The innovation of u-shapelets is its knowingly disregarding maximum information, and merely employ a small number of subsequences for grouping. The advantages of U-Shapelets over shapelets are:

1. It is determined for data samples where the discrete elements are of diverse lengths.
2. It alleviates sensitivity to inappropriate information like noise, spikes, dropouts, etc.
3. This revealed the capability to offer added insights into the data.

3.1 Definition and Background

Definition 1: “Time-Series, $TS = TS_1, TS_2, TS_3, \dots, TS_n$ is a well-arranged collection of physical values. The real values are equivalent to the dimension of Time-Series. A data sample $D = \{TS_1, TS_2, TS_3, \dots, TS_n\}$ is a group of N Time-Series. From [23], it is inferred that the small subsequences that best represents its clusters might give improved bundling results compared to employing whole Time-Series.

Definition 2: Subsequence, a subsequence $SQ_{i,l}$, where $1 < l < n$ and $1 < i < n$, is a bunch of l uninterrupted real values from Time-Series TS and initiates at location i . Time-Series of size n has $\frac{n(n+1)}{2}$ subsequences of entire probable dimensions. For N Time-Series in the data sample having the size n , formerly there are $N \times \frac{n(n+1)}{2}$ subsequences.

Definition 3: The Subsequence distance amongst a subsequence SQ of size m and a Time-Series TS of size n is the distance amongst SQ and the subsequence of TS having minimal distance. It is referred to as $sqdis(SQ, TS)$.

$$sqdis(SQ, TS) = \min_{1 \leq i \leq n-m} dis(SQ, TS_{i,m}); \quad [1 \leq m \leq n] \quad (1)$$

Definition 4: An *unsupervised-shapelet* is a subsequence of a Time-Series TS where the sdists amongst Time-Series from a group D_x are reduced compared to the sdists amongst and remaining group D_y in the data sample D .

$$sqdis(\hat{S}Q, D_x) \ll sqdis(\hat{S}Q, D_y) \quad (2)$$

The matrix comprises of the $sqdis$ vectors amongst u-shapelets and every Time-Series in data sample at a Distance map.

Definition 5: A *Distance map* includes $sqdis$ amongst every u-shapelets and entire Time-Series in the data sample. If there are m u-shapelets for a data sample of N Time-Series, the dimension of the distance map is $[N \times m]$ where every column is a distance-vector of a u-shapelets” [24].

4. DTW Based U-Shapelets Clustering Algorithm

In the paper, the author presented a novel clustering technique specifically for various kinds of Time-Series data samples. Different from existing shapelets that are employed for the classification of Time-Series data samples, in this approach, unsupervised Shapelets (u-Shapelets) [23] are used merely for the clustering of the data samples. The unsupervised shapelets are extracted without the use of any class labels for the data samples. In this approach, every entity in the samples is a Time-Series, which are of dissimilar size. Initially, as to perform the clustering technique, u-shapelets are extracted from the numerous time-series data samples. This technique clusters the data based on the u-shapelets extracted from the entire Time-Series datasets using the DTW similarity measure and explicitly allows us to ignore some of the information that is not extracted by the u-shapelets such as outliers. The proposed approach is represented in the Figure.2. The proposed clustering algorithm is comprised of two different phases. They are

1. Extraction of U-Shapelets by ignoring the outliers

2. Clustering of Time-Series data using DTW Similarity Measure

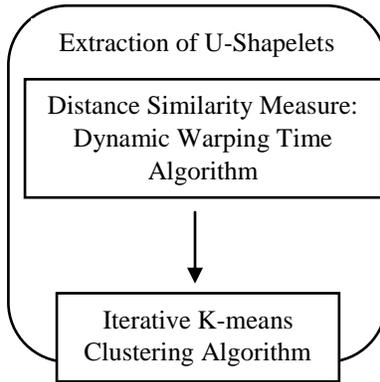


Figure 2: Time-Series Clustering using U-Shapelets with DTW measure

The novelty of this clustering algorithm lies in both the extraction of u-shapelets and the clustering of data. For both these phases, it is essential to use an efficient similarity measure. As given in the previous section that, it is beneficial to employ u-shapelets for clustering purposes instead of simply using the different similarity measures. A similarity measure on Time-Series data series hereafter is further complex to determine compared to traditional informationsince the order of objects in the seriesneeds to be considered. Thus, a non-linear similarity measure is used in the proposed approach instead of linear Euclidian Distance.

4.1 Computation of DTW similarity Measure

The DTW technique depends on the Levenshtein distance and was suggested for appliances in speech recognition. It defines the optimumarrangementamongst two series of arithmeticalvalues and seizesstretchable resemblancethrough aligning the coordinates within both series. However, DTW does not fulfill the Triangle Inequality property of a Metric Distance Measure, it is useful in comparing time-shifted, stretched, or dilated two unequal length signals. Consider two-timesequences P and Q of size M and N correspondingly. Let $P = P_1, P_2, P_3, \dots, P_M$ be a series of M examples of the 1-dimensional indicator. Let $Q = Q_1, Q_2, Q_3, \dots, Q_N$ be a series of N examples of the other 1-dimensional indicator. DTW uses 2 stages to calculate the warppathway between the 2 sequences. Stage 1 consequences in a matrix of local costs $C(i, j)$ of magnitude $N \times M$ by means of Minkowski distance measures as in Equation 1. Stage 2 consequences a matrix of universalcosts $D(i, j)$ of magnitude $N \times M$ using local distances as in Equations 2,3, and 4. In stage 1, the Local cost matrix is estimated employing Minkowski distance measure as “ :

$$C(i, j) = \|P_i - Q_j\| \tag{1}$$

In stage 2, the initialrow of the universal distance matrix is evaluated through accumulative summing of local distances of the row as:

$$D(1, j) = \sum_{k=1}^j C(P_1, Q_k) \text{ for } j \in [1, M] \tag{2}$$

Then the First column of the global distance matrix is calculated by the cumulative sum of local distances of the column as in Eq.3

$$D(i, 1) = \sum_{k=1}^j C(P_k, Q_1) \text{ for } i \in [1, N] \quad (3)$$

For the remaining elements, for i in $[2, N]$, and j in $[2, M]$, the global distance matrix is calculated as in Eq. 4.

$$D(i, j) = \min[D(i - 1, j - 1), D(i - 1, j), D(i, j - 1)] + c(P_i, Q_j) \quad (4)$$

A warping path W is a contiguous set of matrix elements that defines a mapping between two Time-Series' P and Q . After computing the Global distance matrix, a warped path is found from $D(1, 1)$ to $D(N, M)$ ^[25].

For any data sample, once the distance map of the u-shapelets' distances is obtained, it could flexibly move into a standard clustering approach known as k-means. Therefore, the concentration of the study is in approaches to attaining high valued distance maps. Consider that the distance map demonstration is slightly identical to the vector space prototype, which is a keystone for maximum text mining approaches^[26].

4.2 Extraction of U shapelets

The higher-level notion of the proposed approach is that it searches for the u-shapelets that could divide and eradicate a subset of Time-Series from remaining data samples, the generatively recaps this exploration amongst the remaining information till no data left over as separated. The algorithm for the extraction of u-shapelets is given where the distance between the subsequences is evaluated using DTW similarity Measure. This algorithm is viewed as a greedy search approach that tries to exploit the departure gap amongst two subsets of D . Algorithm 1 gives the approach for the extraction of u-shapelets from the Time-Series data sets and Algorithm 2 specifies the approach for the computation of distances between the Time-Series objects using u-shapelets employing DTW algorithm.

The maximum gap is computed and dt of a candidate u-shapelets where the distance vector of applicant u-shapelets. Then, the gap is computed for every possible location dt . The distance vector consumes a series and data sample as input and computes sequence distance amongst subsequence and every Time-Series in the data sample.

Algorithm 1: Extraction of U-Shapelets

Input: D : dataset, $stlen$: Shapelet Length

1. Initialize the set of u-shapelets as an empty sequence $S^Q = []$
2. A Time-Series(ts) dataset is considered $ts = D(1, ;)$
3. While true
 - a. $count = 0$
 - b. $s^q = []$
 - c. For $seq_l = sqlen(1)$ to $sqlen(end)$

- i. For $i = 1$ to $|ts| - seq1 + 1$
 - $\hat{s}q(count + 1) = ts(i:i + sl - 1)$
 - $[sgap(count + 1), dt(count + 1)] = (computesGap(\hat{s}q(count + 1), D))$
 - d. $ind = \max(sgap)$
 - e. $\hat{S}Q = \hat{s}q(ind)$
 - f. $distance = compute\ distance(\hat{s}q(ind), D)$
 - g. $D_A = compute\ (distance < dt)$
 - h. If $len(D_A) == 1$ break
 - i. Else
 - i. $index = \max(distance), ts = D(index)$
 - ii. $\emptyset = mean(distance_{D_A}) + std(distance_{D_A})$
4. Return $\hat{S}Q$

Algorithm 2: Computing the distance between shapelets and dataset

Input: $\hat{s}q = subsequence, D = Dataset$

Output: $distance = distances$ from the whole sequence in the data sample.

1. $distance = []$
2. $\hat{s}q = zNorm(\hat{s}q)$
3. for $i = 1$ to $|D|$
 - a. $ts = D(i, :); distance(i) = inf$
 - b. for $j = 1$ to $|ts| - |\hat{s}q| + 1$
 - i. $z = zNorm(ts_{j,|\hat{s}q|})$
 - ii. $d = DTWDistance(z, \hat{s}q)$
 - iii. $distance(i) = \min(d, distance(i))$
4. Return $distance / \sqrt{|\hat{s}q|}$

4.3 Clustering of Time-Series

The clustering of the Time-Series dataset with the extracted unsupervised shapelets is done employing the iterative k-means approach by computing objective function employing DTW and keeping clusters that minimize it. The algorithm for clustering of Time-Series is given algorithm 3.

Algorithm 3: Clustering the dataset using iterative k-means approach

Input: D : Data sample, $\hat{S}Q = group\ of\ u - shapelets, k = number\ of\ clusters$

Output: $cluster$: Cluster label for every time series

1. $Dis_{MAP} = []$
2. $Cluster(0) = c$
3. For $count = 1$ to $length(\hat{S}\hat{Q})$
 - a. $s\hat{q} = \hat{S}\hat{Q}$
 - b. $distance = [Dis_{MAP} \text{ distance}], sumDis_{MAP} = inf$
 - c. For $i = 1$ to n
 - d. $[Ind, SumD] = k - means(Dis_{MAP}, k)$
 - e. if $sum(SumD) < sumDis$
 - i. $sumDis = sum(SumD)$
 - ii. $cluster(count) = Ind$
 - f. $RI_c = 1 - RI(Cluster(count - 1), Cluster(count))$
4. $a = \min(RI_c)$
5. Return $Cluster(a)$

5. Experimental Results and Its Analysis

The experimental results for suggestedTime-Seriesclustering using u-supervised shapelets are performed on the using Matlab r14b version. The time-series data sets that are considered in this suggested technique are Four Classes, Trace, PAMAP, and Birds that are collected from different data repositories. For further details and data, itself is also found in supporting page ^[27].The complete information pertaining to the experimented data samples are given in Table 1.

Table 1: Experimental Data Samples

Dataset	No. of Time-Series	Time-Series Length	No. of Classes
Four Classes	200	275	2
Trace	200	275	4
PAMAP	345	500	7
Birds	177	500	2

Numerous Diverse metrics for estimating the eminence of Time-SeriesgroupingcomprisesJaccard Score, F1-Score, Rand Index, Folkes and Mallow Index, etc. In this proposed approach, the Rand Index is considered for analyzing the proposed approach. This Index is the most generallyemployed clustering quality metric.

Consider $C = C_1, C_2, \dots, C_m$ is a grouping outline of sample X and $P = \{P_1, P_2, \dots, P_s\}$ is a determinedsegment. Collection of points (X_v, X_u) are referred from the sample employing the below terms:

- SS: if both points fit a similar group of the clustering outline C and to a similar set of fragments P.
- SD: if points fit similar to group C and diverse set P.
- DS: if points fit diverse group C and to similar set P.
- DD: if both points fit diverse group C and to diverse groups P.

Let us assume that a, b, c, and d represent the values for SS, SD, DS, and DD correspondingly. Here $a+b+c+d=M$ which is the maximal of the entire data sample. Thus, the Rand Index (RI) or Rand Statistics that measure the degree of similarity amongst C and P is computed as:

$$RI = (a + d) / M$$

The outcome given does not specify the execution time for the algorithms, since the approach optimizes only for the Quality not for time. The underlying clustering algorithm used is k-means where the accurately right value of k is given and reported the finest of twenty executions. The finest gives the execution that diminished the objective function, prior to the classes are seen and Rand Index is computed. Table 2 showed the clustering quality of u-shapelets employing existing Euclidean distance measure and proposed DTW distance measure. From the table, it can be inferred that the rand index quality measure for the proposed DTW based U-Shapelets Time-Series clustering is high when compared to the existing ED-based U-Shapelets Time-Series clustering. The Rand Index measure equal to 1 signifies a good clustering approach in the Time-Series analysis. The best U-Shapelets extracted from the proposed approach for the Four Classes, Traces, and Birds Data Samples are shown in Figure 3, Figure 4, and Figure 5.

Table 2: Comparison of Rand Index Values

Dataset	Rand Index	
	U-Shapelets with Euclidean Distance	U-Shapelets with DWT measure
Four Classes	1	1
Trace	1	1
PAMAP	0	
Birds	0.642	0.752

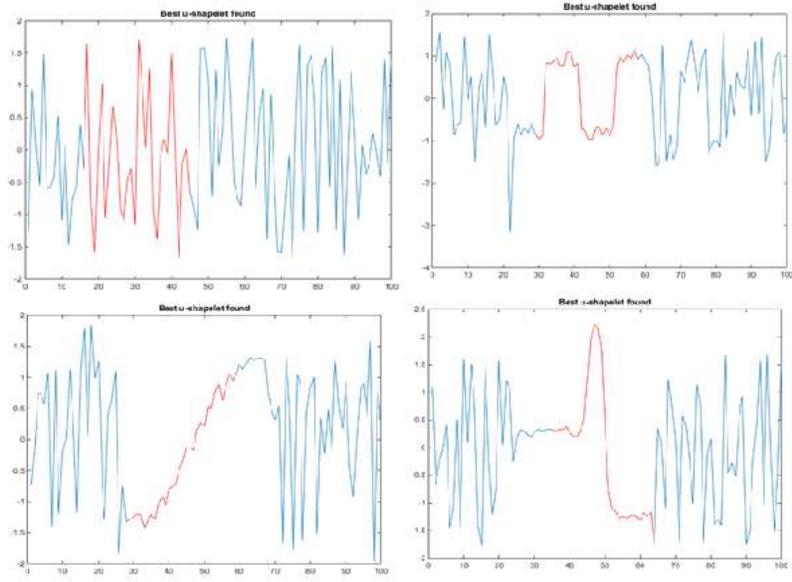


Figure 3: Best U-shapelets found in Four Classes Data Sample

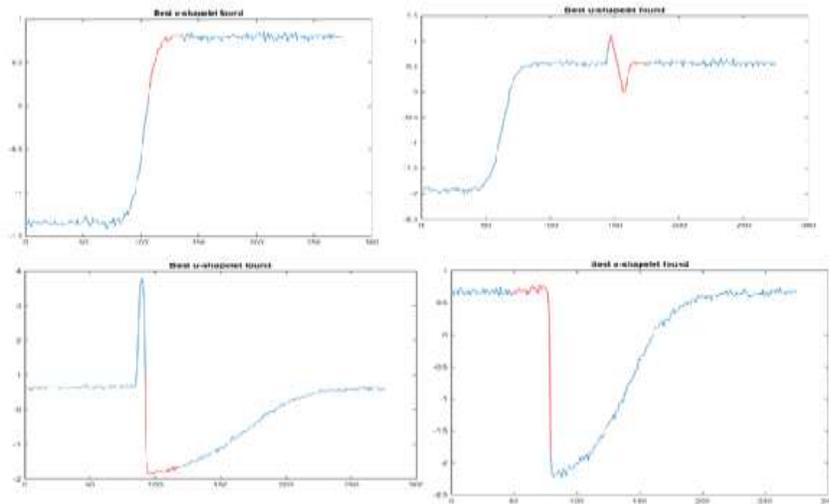


Figure 4: Best U-shapelets found in Trace Data Sample

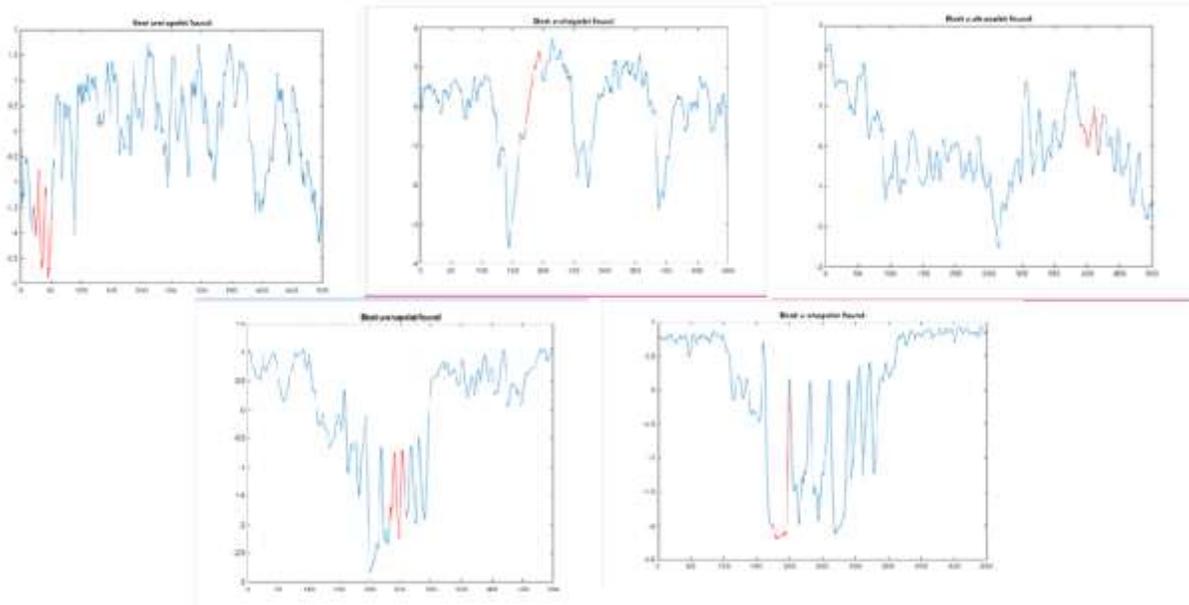


Figure5: Best U-Shapelets obtained for the Birds Data Sample

6. CONCLUSIONS

Clustering Time-Series is a significant area inspired through numerous investigating demands comprising identical exploration in addition to challenges of generating approaches to distinguish dynamic changes in Time-Series. In this paper, a novel methodology is suggested to cluster the Time-Series data samples employing extracting u-shapelets from using the dynamic and efficient similarity measure. The dynamic time warping algorithm is employed as a similarity measure for extracting u-shapelets. This measure gave better accuracy and efficacy in forming the clusters when compared to the existing Euclidean distance measure. The DTW algorithm can be used for the data samples having different Time-Series lengths which are one of the advantages compared to ED measure. However, the computation time is more in the case of the DTW approach. The quality of the clustered data samples is measured using the Rand Index Approach and results showed that the DTW based TS clustering approach has a higher value compared to the ED measure.

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